DOCUMENT RESUME

ED 218 097

SE 037 897

AUTHOR TITLE

Dershem, Herbert L.

Computer Problem Solving. [and], Iteration and

Computer Problem Solving. Computer

Science/Algorithms. Modules and Monographs in Undergraduate Mathematics and Its Applications

Project. UMAP Units 477 and 478.

INSTITUTION P SPONS AGENCY

Education Development Center, Inc., Newton, Mass.

National Science Foundation, Washington, D.C.

PUB DATE

GRANT SED-76-19615-A02

NOTE'

75p.

EDRS PRICE DESCRIPTORS MFOT Plus Postage. PC Not Available from EDRS. *Algorithms; Answer Keys; *College Mathematics; Computers; *Computer Science Education; Higher Education; Instructional Materials; *Learning Modules; *Mathematical Applications; *Problem Solving; Supplementary Reading Materials

ABSTRACT

These modules view aspects of computer use in the problem-solving process, and introduce techniques and ideas that are applicable to other modes of problem solving. The first unit looks at algorithms, flowchart language, and problem-solving steps that apply this knowledge. The second unit describes ways in which computer iteration may be used effectively in problem solving, and shows ways in which two other forms of iteration may be applied in algorithm construction. Both modules include exercises, and each has a model exam. Answers to all problems presented are provided. (MP).

Reproductions supplied by EDRS are the best that can be made from the original document. ******* *********

U.S. DEPARTMENT OF EDUCATION
NATIONAL TINSTITUTE OF EDUCATION
EDUCATIONAL RESOURCES INFORMATION
CENTER (ERIC)

- his document has been reproduced as received from the person or organization
- Minor changes have been made to improve
- reproduction quality

 Points of view or opinions stated in this docu ment do not necessarily represent official NIE COMPUTER PROBLEM SOLVING

Herbert L. Dershem Department of Computer Science Hope College Holland, Michigan 49423

MODULES AND MONOGRAPHS IN UNDERGRADUATE MATHEMATICS AND ITS APPLICATIONS PROJECT

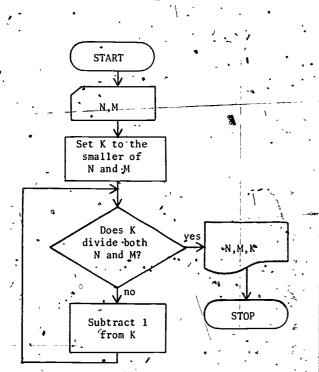
"PERMISSION TO REPRODUCE THIS MATERIAL IN MICROFICHE ONLY HAS BEEN GRANTED BY

COMPUTER PROBLEM SOLVING

by Herbert L. Dershem

TO THE EDUCATIONAL RESOURCES INFORMATION CENTER (ERIC)."

, TABLE OF CONTENTS



COMPUTER SCIENCE/ALGORITHMS

edc/umap/55chapelst/newton/mass.02160

1. INTRODUCTION . 2. ALGORITHMS . .

SOLUTIONS TO MODEL EXAM

Intermodular Description Sheet: UMAP Unit 477

Title: COMPUTER PROBLEM SOLVING

Author: Herbert L. Dershem
Department of Computer Science
Hope College

Holland, Michigan 49423/

Review Stage/Date: 'III 9/30/80

Classification: COMPUTER SCLALGORITHMS

'Írerequisite Skills: None

Output Skills:

- Be able to explain the concept of algorithm and be able to distinguish algorithms from non-algorithmic solution descriptions.
- Be able to read and explain algorithms written in the flow chart language.
- 3. Be able to state the seven steps in computer problem solving and be able to apply them in solving simple problems.

Related Units

Iteration and Computer Problem Solving (Unit 478)

© 1980 EDC/Project UMAP All rights reserved.

MODULES AND MONOGRAPHS IN UNDERGRADUATE MATHEMATICS AND ITS APPLICATIONS PROJECT (UMAP)

The goal of UMAP is to develop, through a community of users and developers, a system of instructional modules in undergraduate mathematics and its applications which may be used to supplement existing courses and from which complete courses may eventually be built...

The Project is guided by a National Steering Committee of mathematicians, scientists, and educators. UMAP is funded by a grant from the National Science Foundation to Education Development Center, Inc., a publicly supported, nonprofit corporation engaged in educational research in the U.S. and abroad.

PROJECT STAFF

Ross L. Finney Solomon Garfunkel Felicia DeMay Barbara Kelczewski Paula M. Santillo Donna DiDuca Janet Webber Zachary Zevitas

Director
Gonsortium Director
Associate Director
Coordinator for Materials Production
Assistant to the Directors
Project Secretary/Production Asst.
Word Processor
Staff Assistant

NATIONAL STEERING COMMITTEE

W.T. Martin (Chair).
Steven J. Brams
Llayron Clarkson
Ernest J. Henley
William Hogan
Donald A. Larson
William F. Lucas
R. Duncan Luce
George Miller
Walter E. Sears
George Springer
Arnold A. Strassenburg
Alfred B. Willcox

M.I.T.

New York University

Texas Soluthern University
University of Houston
Harvard University

SUNY at Buffalo
Cornell University
Harvard University
Nassau Community College
University of Michigan Press
Indiana University
SUNY at Stony Brook
Mathematical Association of America

The Project would like to thank Carol Stokes of Danville Area Community College, Danville, Illinois; Ray Treadway of Bennett College, Greensboro, North Carolina; Douglas F. Hale of the University of Texas Permian Basin, Odessa, Texas; Carroll O. Wilde Off the Naval Postgraduate School, Monterey, California; and one anonymous reviewer, for their reviews, and all others who assisted in the production of this unit.

This material was prepared with the partial support of National Science Foundation Grant No. SED76-19615 A02. Recommendations expressed are those of the author and do not necessarily reflect the views of the NSF or the copyright holder.

1. INTRODUCTION

Much of a person's life is spent in solving problems. Usually, we use a tool or a set of tools to assist us in solving those problems. For example, when faced with the problem of transporting myself from where I am now to a focation across town where I would like to be, I might use an automobile as a tool. If I am faced with the problem of removing the contents of a capped bottle, a bottle-opener would be an appropriate tool. In some cases, I need to use a combination of tools. For example, if I had to remove the contents of a capped bottle that was in a store across town, I would use both the automobile and the bottle-opener.

For many problems that people need to solve, the computer is an appropriate tool. But the computer is just a tool; it will not solve a problem by itself. The computer can assist you in solving a problem only if you know how to utilize it correctly. This module introduces techniques and ideas which you may apply when using the computer to solve problems.

Although we are primarily concerned with the use of computers in the problem solving process, the techniques are applicable to other modes of solving problems.

ALGORITHMS

The first task in solving a problem is finding appropriate ways of representing the solution process. The more carefully this is done, the easier the problem solving process. An algorithm is a common way of representing the solution process, so we begin by defining this term.

Definition of an Algorithm

An ordered set of rules for solving a problem is called an algorithm if it has the following properties:

- 1. The rules are unambiguous.
- 2. The rules are in a proper sequence.
- The procedure specified by the set of rules solves the problem.
- 4. The procedure terminates after a finite number of steps, or actions specified by the rules,

We will "back into" an understanding of what an algorithm is by first considering what one isn't.

Nonalgorithm 1. Directions for getting to the hospital.

- Go west on Tenth Street until you come to a stoplight.
- 2. Turn onto River Avenue at the stoplight.
- 3. Make a right at the Y on River Avenue.
- 4. The hospital will be on your right a few blocks past the Y.

Unfortunately, we have all been the recipients; and probably the givers as well, of nonalgorithmic directions like these. I hope your illness is not too acute in this. case because if it is, you may terminate before the algorithm does. The problem with this nonalgorithm is that it violates condition 1 by being ambiguous. In rule 1, which stop light is meant? In rule 2, which way should I turn? At the Y described in rule 3, there is a right fork and a sharp right turn possible. Which should I take? How many blocks are a few in step 4?

Nonalgorithm 2. Directions for passing an exam.

- I. Get lots of sleep the night before the exam.
- 2. Outline the material.
- 3. Read the material.
- 4. Listen attentively in class.
- 5. Take the examination.

This nonalgorithm contains rules that might be adequate to solve the problem, but they cannot be carried out in the specified order. Thus the rules are not in proper sequence, and condition 2 of the algorithm definition is violated.

Nonalgorithm 3. Directions for passing a true-false test

- '1. Bring a coin to the testor.
- 2. Flip the coin for each item on the test.
- 3. If the coin lands heads respond with true, if

There is no ambiguity in this nonalgorithm, and steps are in proper sequence. The only difficulty is that unless you have an unusually intelligent (lucky?) coin, this procedure may not solve the problem at hand, which is to pass the test. Hence, condition 3 of the definition is violated.

Nonalgorithm 4. Directions for making a million dollars.

- 1. Get 10 million dimes.
- 2. Go to Las Vegas.
- 3. Play the dime slot machines until either you have 20 million (or more) dimes or until you, run out of them.
- If you run out of dimes, go back to step 1.
- 5. If you reach 20 million dimes, quit while you're ahead! . . .

Even if you obtain the supply of dimes needed in step 1 and the cranking power needed in step 3, this procedure is still a nonalgorithm because it may never terminate: there is no guarantee that you will ever obtain the desired result at step 3. Hence, condition 4 in the definition is violated.

Now we are ready to consider an example which does qualify as an algorithm under our definition.

Algorithm 1: Find the greatest common divisor of two given numbers, N and M.

- 1. Let K be the smaller of N and M.
- 2. If K divides both N and M, then K is the greatest common divisor.
- 3. Otherwise, subtract 1 from K.
- 4. Go to step 2.

This algorithm is unambiguous, its rules are in proper sequence, it solves the problem, and it does so in a finite number of steps. It is also very simple and easy to follow. However, it may take a long time to solve the problem using this algorithm. For example, if 15798433 and \$66832 are used for N and M, step 2 would be executed \$66783 times before the correct answer of 49 is found. A more efficient algorithm, that is, one that can solve the same problem with much less effort, is known and we shall present it next.

Algorithm 2. Given two numbers, N and M, find their agreatest common divisor.

- 1. If N is smaller than M, then exchange the two:
- 2. Divide N by M and call the remainder R.
- 3. If the remainder R is zero, then M is the GCD.
- 4. Otherwise, set N to the value of M and M to the value of R.
- 5. Go to step 2.

If we follow this algorithm for N = 15798433,

 $M \leq 566832$

M = 493969

 $^{-}M = 72863$.

M = 56791

M = 16072

M = 8575

M = 17497

7

M = 1078 M = 1029

'In this case we execute step 2 only nine times, a significant improvement over Algorithm 1.

The phenomenon which we observe here occurs often in algorithms. Algorithm-1 is simple, straightforward, and solves the problem in an inefficient manner. Algorithm 2 is much more efficient but the cost is additional difficulty in understanding it. This tradeoff between simplicity and efficiency of algorithms frequently forces the algorithm designer to make a decision on the subject of priorities.

Exercises

- 1. Modify nonalgorithm 2 to make it an algorithm.
- 2. Determine whether each of the following are algorithms or non-algorithms. For each nonalgorithm, find the rule or rules it violates and rewrite it as an algorithm.
 - (a) How to place a telephone call.
 - 1. Pick up the receiver.
 - 2. Listen for a dial tone.
 - 3. Dial the number.
 - 4. Conduct the conversation.
 - (b) How to find a word in a dictionary or determine that it is not listed.
 - 1. Turn to any page.
 - 2. If word at the top left of the page occurs alphabeticallly after the desired word, go to step 4.
 - 3. Turn ahead 10 pages and go to step 2.
 - 4. Turn back 2 page's.
 - 5. If word at the top right is before the desired word, go to step 3.
 - 6. Scan page for desired word.
 - 7. If it is found, write a definition.
 - B. If it is not found, write, "not in dictionary."

- (c) How to fill a ditch with sand.
 - 14 Obtain a shovel.
 - 2. Start shoveling sand into the ditch.
 - 3., If you run out of sand, go get more and go to step 1.
 - 4. When ditch is full, stop.
- (d) How a doctor heals a patient.
 - 1. Learn about patient's problem.
 - 2. Consider the symptoms.
 - 3. Initiate a treatment.
 - 4. Examine and test patient.
- . 5. If patient is cured, then send the bill.

3. FLOWCHART LANGUAGE

We next ask how we should express algorithms. In other words, is there a convenient language for communicating an algorithm from one person to another or from a person to a computer?

The language we have used above in communicating. Algorithms 1 and 2 is English, which is very appropriate because it is understood by a reasonably large subset of the people with whom we communicate. English has two disadvantages, however. First, it is ambiguous as far as meaning is concerned, and therefore, even a carefully worded algorithm can suffer from the ambiguity of the language. Second, English is not an appropriate language for communicating with computers, since it is too complicated for them to understand.

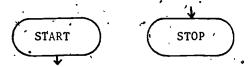
It would appear then, that a computer programming language may be an answer to our dilemma. Programming languages are, of necessity, unambiguous, and are understandable to the computer. And indeed one of our goals is to express algorithms in this form so that the computer can solve the problem. But people have difficulty expressing algorithms directly in programming.

languages. For this reason we develop an intermediate language between English and the programming language, which we call *Plowchart Language*.

The expression of an algorithm in Flowchart
Language consists of the rules of the algorithm written
in abbreviated English and pictured graphically in
"boxes." These boxes are connected by arrows which
indicate the sequencing of the steps. We will use this
Flowchart Language to express all of our algorithms.

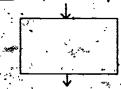
There are five different kinds of boxes that are used in representing algorithms.

1. Terminal box



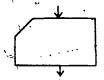
Terminal boxes are used to identify the starting point and stopping point of an algorithm. They will always contain either the word START or the word STOP.

2. Processing box



The work of the algorithm is specified in processing boxes. It contains an English statement which describes the action that is to be taken.

3. Imput box

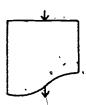


Each input box contains the names of variables whose values are to be obtained from a known source. For example, the box



represents the obtaining of two values, the first called N and the second M.

4. Output box

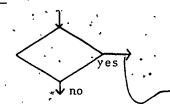


Like an input box, each output box contains the names of variables. The values of these variables are to be displayed in some form. To example, the box



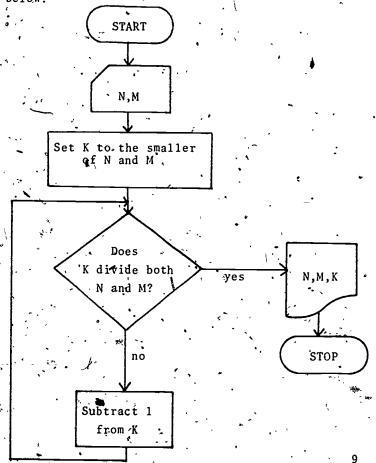
indicates that the current value of X is to be displayed.

5. Decision box



Each decision box contains a question which can be answered yes or no. If the answer is "yes," the "yes" path is taken from the box. If the answer is "no," the "no" path is taken:

As an example, Algorithm 1 in Flowchart Language is shown below.



Names that are used in an algorithm to represent numerical values and whose values may change during the execution of the algorithm, are called variables. Three variables, N, M, and K, are used in Algorithm 1. It is easier to understand what an algorithm does if there is some explanation of the meanings of the variables included with the algorithm. For example, for Algorithm 1, our variable descriptions would be as follows:

Variables

Name N,M Descriptions :

K

The two given numbers.

A counter—used in searching for the greatest common divisor. It will contain the greatest common divisor when the algorithm terminates.

Setting a variable to the value of another variable or to the result of some arithmetic expression is such a common algorithm step that a special symbol, the left pointing arrow, is used to represent it: For example,

Δ+R

means "set A to the value of B." This notation can also be used to represent the incrementing or decrementing of variables. The step "add 1 to X" is given by

X+X+1

Using this new symbol and the variable descriptions, we can now restate Algorithm 1.

Algorithm 1 - Second Version. Given two numbers, and M. find their greatest common divisor.

<u>Variables</u>

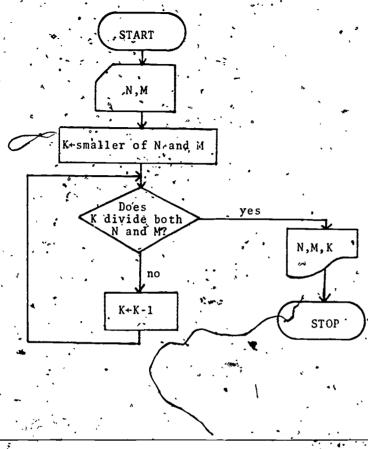
N,M'

Description

The two given numbers.

A counter used to search for the greatest

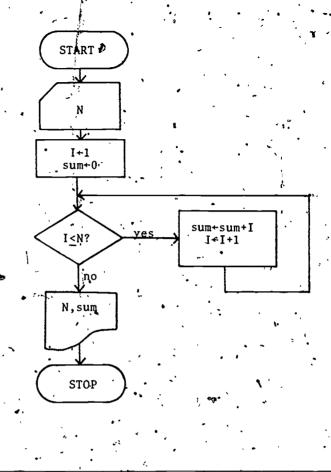
common divisor. It will contain the greatest common divisor when the algorithm terminates.



Exercises

- 3. Write algorithm 2 in the Flowchart Language.
- 4. Follow the algorithm described in the following flowchart and give the resulting output when the input value is 5.

		variables
-	Name .	Descriptions
,	N .	The number input.
	I í	A counter.
,	Sum	The sum of the first N integers



4. PROBLEM SOLVING STEPS

Now that we have the concept of an algorithm and the flowchart language available, we are ready to learn how to use these tools in solving problems. It would be simple if we could put the statement of a problem into a machine and get out an algorithm for solving it. Unfortunately, no such machine has ever been discovered. Problem solving is accomplished only through careful work: before the algorithm is constructed, detailed planning and analysis must occur; after the algorithm is constructed,

extensive testing must take place to verify that it does indeed solve the problem.

In this section we outline a step-by-step procedure that is useful in the construction of algorithms which solve problems. You might call this an algorithm for constructing algorithms. This process consists of seven steps which are described below.

1. Precisely define the problem.

At this step, the problem solver determines what the problem is. This step, in practice, is usually quite difficult. In many courses we are not concerned with this step since the problems are precisely formulated by the textbook author or the instructor. An important part of this step is determining exactly what form the output of the problem should have.

2. Identify the inputs to the problem.

At this step you ask, "What are the pertinent facts that are given in this problem?" The answer will depend on what is available and what is needed. One important aspect of this task is determining the appropriate form for the input.

3. Identify the outputs of the problem.

Here you determine the results that are desired. By considering the result of step 1, you should be able to determine what is needed and in what form.

4. Construct an algorithm for the solution.

This is the key step in the process and one which can cause the most trouble. Too many problem-solvers try to skip this step or combine it with the next in an effort to obtain a solution quickly. This is a situation where haste really does make waste: time invested in careful formulation here can save much more time at steps 6 and 7.

5. Implement the algorithm for the solution.

In computer problem solving, this step is known as programming. If step 4 is done carefully, it can be carried out in a straightforward way once the basics of a programming language are mastered.

6. Test the procedure constructed in step 4.

Once the implementation is complete, we test the procedure using inputs for which the correct outputs are known, and compare the results with our expectations. If they differ, then the existence of an error has been discovered. There is a temptation to assume the algorithm is correct and rush through this step. As you gain-more, experience with computer problem solving, you will learn (probably the hard way) that you should never assume anything is correct. That kind of skeptical attitude makes for the best testing.

7. Locate and correct errors uncovered by testing and go back to step 6.

Errors may originate at step 4 or step 5. Usually those which originate at step 5 are fairly easy to detect and correct because they require some minor modification to the program. Errors which originate at step 4 are much mome difficult. Such errors may require you to completely rethink your algorithm and, in some cases, discard all you have done and start over. Again, a careful job at step 4 can avoid this waste.

5. AN EXAMPLE

Let's follow this process through for a simple problem. The problem is to read a set of numbers and determine how many are positive and how many are negative.

 Precise formulation - The problem as stated above leaves out some necessary information. First, what are we to do with zeros? Should they count as positive, negative, or not at all? Secondly, how will we know when we have all of the numbers?

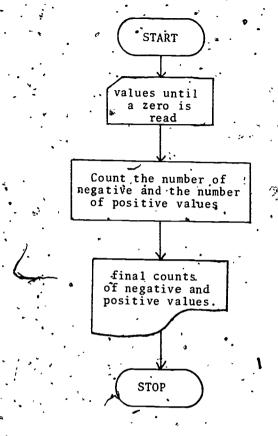
We can solve both of these problems at once by saying a zero will not be counted as positive or negative but rather a zero will signify the end of the data.

Therefore, our more precise formulation of the problem now reads as follows:

Read a set of numbers until a zero is encountered and count the number of positive and negative numbers read.

- Inputs The inputs will be the given set of numbers, all non-zero, followed by a zero. Note that any input not ending with a zero is invalid for this problem.
- 3. Output The output of our problem consists of two numbers, the number of positive values and the number of negative values.
- 4. Construction of an algorithm · Our flowchart language is a useful tool here and we can nicely formulate our solution as follows:

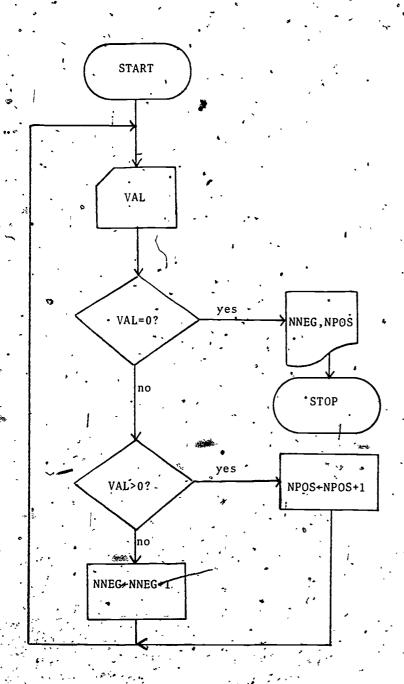
Algorithm 2. Count the number of positive and negative values in a data/set - Version I.



This solution algorithm, though certainly correct, provides too little detail to be of sufficient use in implementation. Therefore, we refine it.

Algorithm 3. Count the number of positive and negative values in a data set - Version II.

Name	•	Description
VAL		The values input.
NNEG	•	The number of negative values.
NPOS		The number of positive values.



This algorithm appears to be correct. But as we warned earlier, never assume anything is correct.

- 5. Implementation Algorithms such as this one are implemented translating them into a computer programming language such as FORTRAN or BASIC. Since this module is intended to be independent of programming languages, we will not discuss this step in algorithm development. If you are interested in pursuing this further, you may do so by learning to program in any programming language.
- 6. Testing The above algorithm was implemented in a programming language and run with the following results.

Output: 12,-5,15,-2,7,0
NNEG=1762699507
NPOS=2001731581

Obviously, there is some difficulty here. The strategy used to check for the presence of an error was to use an input for which we know what the output should be. When the output obtained differed from our expectations, we knew there was an error, and therefore we must proceed directly to step 7.

Had we been successful in generating the expected output for this particular input, we should run additional tests until we have satisfied ourselves that the procedure is correct.

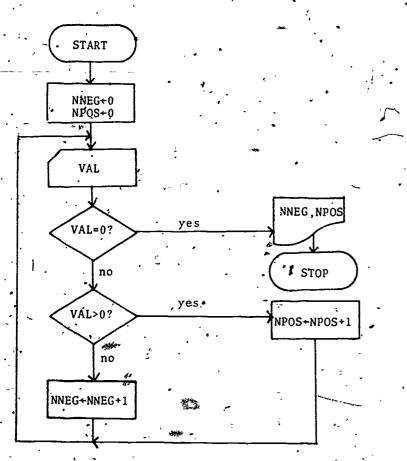
7. Locate and correct errors - This phase of the problem solving process is a difficult one which is learned only through experience. In this case, we notice that values of NNEG and NPOS are quite wild and after a little thought we suspect that these two variables were not given proper initial values, which in this case should be zeros. In many programming languages, variables like NNEG and NPOS are not automatically set to zero. In order to insure the correctness of our

program we need to include steps to do this.

After our algorithm is modified to include these initializations to zero, it takes the following form.

Algorithm 4. Count the number of positive and negative values in a data set - Version 3.

Name	Variables Description							
VĄL,	The values input.							
`NNEG .	The number of negative values.							
NPOS	The number of positive values.							

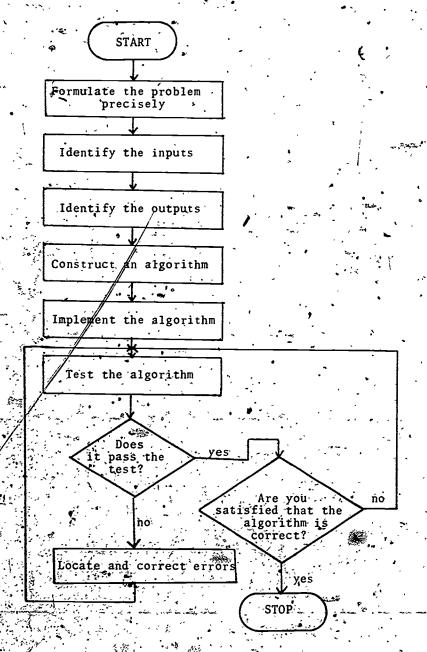


After making the correction which results in Algorithm 4, we must return again to step 6 for testing. Extensive testing of the implemented version of this algorithm will reveal no further errors. When we have tested enough to satisfy ourselves with the correctness of the algorithm, we accept it as providing the solution.

We have now outlined a basic procedure for solving a problem. This procedure can be put in the form of a flowchart as well.

19

÷24



Exercises

Follow through the first four of the seven problem solving steps with the following problems:

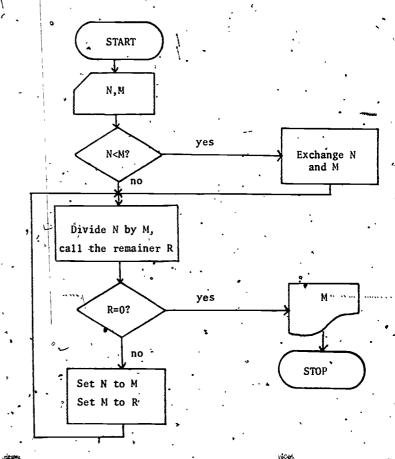
- 5. Put three numbers into non-descending order.
- 6. Calculate the mean of a set of numbers.
- Input an integer and compute the sum of all integers from one to the integer input.
- 8. Input an amount A, and an interest rate I. Compute the principal resulting if A dollars are invested for a given time period.

 with interest rate I percent per time period.
- 9. Input A and I as in 4, and N, the number of time periods.

 Compute the principal resulting if A dollars are invested for N time periods with interest rate I percent per time period compounded after each time period.

6. ANSWERS TO EXERCISES

- 1. One possible solution might be:
 - 1'. Read the material.
 - 2. Listen attentively in class.
 - 3. Outline the material.
 - 4. Gets lots of sleep the night before.
 - 5. Take the examination.
- 2. (a) Nonalgorithm because it may fail to solve the problem.
 For example, what happens if the line is busy?
 - (b) Nonalgorithm because it may not solve the problem. If the search begins on an even (odd) page, then only even (odd) pages will be scanned. If step 4 had read, "Turn back 1 page," the procedure would have been an algorithm.
 - (c) Nonalgorithm because it is ambiguous. Step 3 does not explain how to get more sand.
 - (d) Nonalgorithm because steps are out of order. If steps were changed to 1,4,2,3,5 then it would be better. Also, no action is specified if patient is not dured, so the procedure may not terminate. One could add the step:
 - 6. If patient dies, then stop treatment,



4. This will print

N=5

sim=15

5. Precise formulation: Put three real numbers into non-descending order.

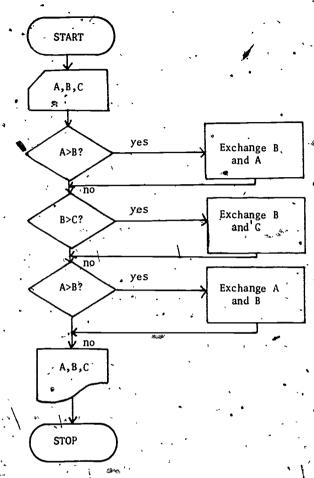
Input: The three numbers in original order.

Output: The three numbers in non-descending order.

Algorithm: <u>Variables</u>

Name Description

A,B,C The three variables read and placed in order with A the smallest and C the largest.



6. Precise formulation: Read a value N, followed by N real numbers and calculate the mean of the N real numbers.

Input: N and N real values.

Output: The mean of the N real plues.

* Variables

Algorithm: Name Description

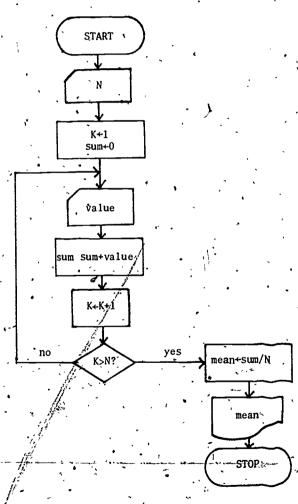
N . The number of values read.

K The counter from 1 to N.

sum . The sum of the values read.

value The values whose mean is computed.

mean The mean.



.31

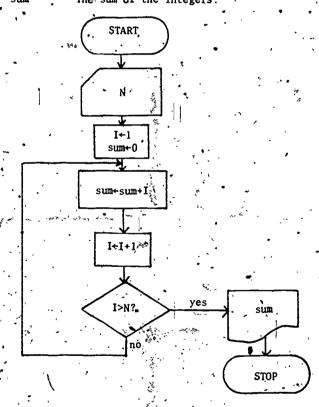
7. Precise formulation: Input a positive integer and compute the sum of all positive integers less than or equal to the integer input.

Input: A positive integer.

Output: The sum of all positive integers less than or equal to the integer input.

Algorithm: Variables

Name	Description •
N	The number of integers summed
Ι	A counter from 1 to
cúm	The cum of the integers



ວ່າ

8. Precise formulation: Given a principal amount A in dollars and an interest rate I in percent per time period, compute the principal at the end of one time period.

Input: Principal amount A and interest rate 4.

Output: Principal after one time period.

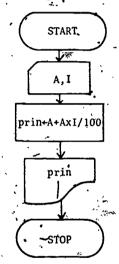
Algorithm: Variables

Name
Description

The amount of beginning principal.

I The interest rate in percent.

prin The amount of principal at the end of the time period.



9. Precise formulation: Given a principal amount A in dollars, an interest rate I in percent per time period, and a number of time periods N, compute the principal at the end of N time periods.

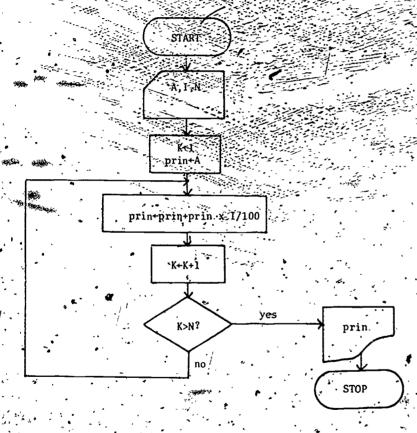
Input: Principal amount A, interest rate I, and number of time periods N.

Output: Principal after N time periods.

Algorithm: Variables

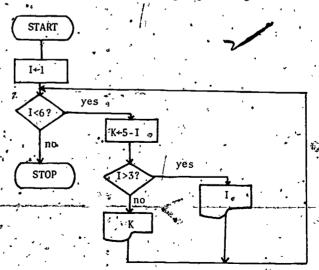
Name Description

- A The amount of beginning principals
- In Interest rate in percent
- N: The number of time periods.
- K A counter from 1 to N
- prin The principal after K time periods.

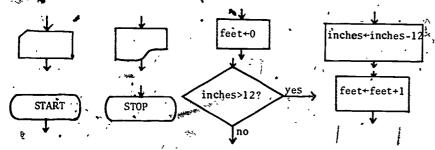


MODEL EXAM

- nonalgorithms. For those that are nonalgorithms, explain why.
 - (a) How to shovel snow off a driveway.
 - 1. Ger-a shovel.
 - 2. Remove a shovelfull of snow from the driveway.
 - 3. If there is still snow on the driveway, go to step 2
 - 4. Stop
 - (b) How to buy a new car.
 - 1. Find-the car you want.
 - 2. Find out its price.
 - 3. Ask your father for the money.
 - 4. Buy the car.
 - (c). How to find a job.
 - 1. Determine which jobs are open.
 - 2. Interview for the jobs you want.
 - 3. Decide which jobs you would like. ..
 - 4. Get the necessary training.
 - 5. Write a resume.
- 2. What output will the following algorithm generate?



- Design an algorithm for solving the following problem: Convert a length from inches to feet and inches.
 - (a) Define the problem more precisely.
 - (b) The following are the boxes needed for an algorithm to solve this problem. Fill in the two empty boxes.



(c) Arrange the boxes above into a flowchart language algorithm to solve the stated problem. Use each box exactly once.

8. SOLUTIONS TO MODEL EXAM

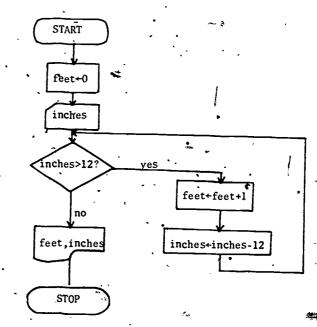
- (a) Algorithm
- '(b) This does not solve the problem. In step 3, you do not receive the money by asking.
- (c) The steps are out of sequence.

. (a) The problem could more precisely say:

Convert a length from inches to feet and sinches where the number of feet is integer and as large as possible.

(b) Input box should contain "inches".

Output box should contain "feet, inches".



Request for Help

Return to: EDC/UMAP . 55 Chapel St. Newton, MA 02160

Student: If you have trouble with a specific part of this unit, please fill out this form and take it to your instructor for assistance. The information you give will help the author to revise the unit.

Your Name		author to revis	e the unit.	Unit No	
Page Upper OMiddle	OR	SectionParagraph	OR	Model Exam Problem No	1
Description of	Difficul	ty: (Please be	*specific)	Problem No.	ļ
		`.·	nem .		•

Instructor:	Plea	se	indicate	you	rr	esolution	of	the	difficulty	in	this	фох.
`	V ,40	٠	٠.	• '	0			1 '				•

Corrected errors in materials. List corrections here:

Gave student better explanation, example, or procedure than in unit.

Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)

38

Instructor's Signature

STUDENT FORM 2

-Unit-Questionnaire

Return to: EDD/UMAP 51.Chapel St. Newton, MA 02160

маше	<u> </u>	_Unit No	Date_		
Institution	8	Course No.			_
Check the choice for ea	ch question that	comes closest t	to Vour personal	opinion.	- · .
1. How useful was the			,	- 0,-1112011,	
	a		• • •	•	٠
Not enough deta			. ` · \	•	٠.
	been clearer wi	th more detail	,		•
Appropriate amo		1.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4.4			•
Too much detail	onally too detai was often di	ted; but this wa	as not distract:	rug	,
100 much, detail	was orten ar	arracted ' '	,		
2. How helpful were th	e problem answer	8?			
	•	-		1	
Sample solution	s were too brief	; I could not do	the intermedia	ate steps	•
	rmation was give				
sample solution	s were too detai	rea; r aranıt	ed them	,	
3. Except for fulfilli	no time prerequis	ites how much d	did von nee oth	er ècurces (for
example, instructor	friends, or ot	her books) in or	rder to underst	and the unit	7
	j , sm 1	, , ,	÷ .	1	÷
A Lot	Somewhat	. 'A Little	e	ot at all	
		3 . 1	1 8 1 8 1 B	· · · · · · · · · · · · · · · · · · ·	_
Wary long was this w	made da composidos				
4. How long was this u	nit in compariso	n to the amount	or time you ger	nerally spen	d. 01
a lesson (lecture a	ind homework assi	gnment) in a typ	pical math or s	cience cours	d· 01 e?
a lesson (lecture a Much	nd homework assi omewhat	gnment) in à tyr About	pical math or se Somewhat	cience cours Much	d· 01 e?
a lesson (lecture a	nd homework assi omewhat	gnment) in a typ	pical math or s	cience cours	d· 01 e?
a lesson (lecture a Much Longer I	and homework assi comewhat conger	gnment) in a tyr About the Same	Somewhat // Shorter	Much Shorter	d· 01 e?
a lesson (lecture a Much Longer I Were any of the fol	and homework assi comewhat conger	gnment) in a tyr About the Same	Somewhat // Shorter	Much Shorter	d: 01 e?
a lesson (lecture a Much Longer I Were any of the fol as many as apply.)	and homework assi comewhat conger	gnment) in a tyr About the Same	Somewhat // Shorter	Much Shorter	d 01 e?
a lesson (lecture a Much Longer I Were any of the fol as many as apply.) Prerequisites	ond homework assi	gnment) in a tyr About the Same the unit confus	Somewhat // Shorter	Much Shorter	d o
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk	ind homework assi comewhat conger lowing parts of	gnment) in a tyr About the Same the unit confus	Somewhat // Shorter	Much Shorter	d o
Much Longer Were any of the fol as many as apply.) Prerequisites Statement on sk Paragraph headi	ind homework assi comewhat conger lowing parts of	gnment) in a tyr About the Same the unit confus	Somewhat // Shorter	Much Shorter	d or
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples	omewhat onger lowing parts of ills and conceptings	gnment) in a tyr About the Same the unit confusi s (objectives)	Somewhat // Shorter	Much Shorter	d of
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista	cond homework assistant descriptions and concept and c	gnment) in a tyr About the Same the unit confusi s (objectives)	Somewhat // Shorter	Much Shorter	d or
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples	cond homework assistant descriptions and concept and c	gnment) in a tyr About the Same the unit confusi s (objectives)	Somewhat // Shorter	Much Shorter	d o
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain	gnment) in a tyr About the Same the unit confusi s (objectives) if present)	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain	gnment) in a tyr About the Same the unit confusi s (objectives) if present)	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.)	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain	gnment) in a tyr About the Same the unit confusi s (objectives) if present)	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please of the fol as apply.) Prerequisites	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain lowing parts of	gnment) in a tyr About the Same the unit confusi s (objectives) if present) the unit particu	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer I Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.) Prerequisites Statement of sk	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain	gnment) in a tyr About the Same the unit confusi s (objectives) if present) the unit particu	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer I Were any of the fol as many as apply.) Prerequisites Statement on sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.) Prerequisites Statement of sk Examples	ind homework assi comewhat conger lowing parts of ills and concept ngs ince Supplement (explain lowing parts of	gnment) in a tyr About the Same the unit confusi s (objectives) if present) the unit particu	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Were any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.) Prerequisites Statement of sk Examples Problems	ind homework assisomewhat longer lowing parts of lils and concept lils and con	gnment) in a tyr About the Same the unit confusi s (objectives) if present) the unit particu	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer I Were any of the fol as many as apply.) Prerequisites Statement on sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.) Prerequisites Statement of sk Examples	ind homework assisomewhat onger lowing parts of ills and conceptings ince Supplement (explain lowing parts of ills and conceptings	gnment) in a tyr About the Same the unit confusi s (objectives) if present) the unit particu	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Much Longer Mere any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e Were any of the fol as apply.) Prerequisites Statement of sk Examples Problems Paragraph headi Table of Content	ind homework assisomewhat conger lowing parts of ills and conceptings ince Supplement (explain lowing parts of ills and conceptings	gnment) in a tyr About the Same the unit confusion s (objectives) the unit particular the unit particular s (objectives)	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?
Much Longer Much Longer Mere any of the fol as many as apply.) Prerequisites Statement of sk Paragraph headi Examples Special Assista Other, please e Mere any of the fol as apply.) Prerequisites Statement of sk Examples Problems Paragraph headi Table of Content	ind homework assisomewhat conger lowing parts of conceptings and conceptings lowing parts of concepting and con	gnment) in a tyr About the Same the unit confusion s (objectives) the unit particular the unit particular s (objectives)	Somewhat Shorter ing or distract	Much Shorter ing? (Check	e?

Please describe anything that you found particularly helpful. (Please use the back of this sheet if you need more space.)

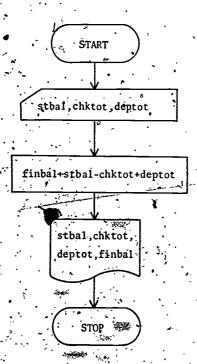
umap

UNIT 478

Modules and monographs in undergraduate mathematics and its applications project

ITERATION AND COMPUTER PROBLEM SOLVING ,

by Herbert L. Dershem



COMPUTER SCIENCE/ALGORITHMS

edc/umap/55chapel st/newton, mass 02160

ITERATION AND COMPUTER PROBLEM SOLVING

by

Herbert L. Dershem Department of Computer Science Hope College Holland, Michigan 49423

TABLE OF CONTENTS

1.	INTRODUCTION	
2.	A MORTGAGE PROBLEM	•
3.`	ITERATIVE IMPROVEMENT	1
4:	ITERATION	. 8
5. ,	VARIABLE-CONTROLLED ITERATION	. 13
	TOP-DOWN APPROACH	. 20
7.	SOLUTIONS TO EXERCISES	. 25
8.	MODEL EXAM	. 29
9.	SOLUTIONS TO MODEL EXAM	. 30

4.1

Intermodular Description Sheet: UMAP Unit 478

Title: ITERATION AND COMPUTER PROBLEM SOLVING

Author: Herbert L. Dershen

Department of Computer Science

Hope College

Holland, Michigan 49423

Review Stage/Date: 9/30/80

Classification: COMPUTER SCI/ALGORITHMS

«Prerequisite Skills:

1. Completion of UMAP Unit 477, "Computer Problem Solving.

Output Skills:

1. Be able to improve algorithms by enhancing them.

- Be able to read, interpret, and follow through (as a computer would) algorithms that involve while, until, and variablecontrolled iteration.
- Be able to describe and apply the top-down appraoch to algorithm design.

Related Units:

Computer Problem Solving (Unit 477)

1980 EDG/Project UMAP All rights reserved.

MODULES AND MONOGRAPHS IN UNDERGRADUATE

"MATHEMATICS AND ITS APPLICATIONS PROJECT (UMAP)

The goal of UMAP is to develop, through a community of users and developers, a system of instructional modules in undergraduate mathematics and its applications which may be used to supplement existing courses and from which complete courses may eventually be built.

The Project is guided by a National Steering Committee of mathematicians, scientists, and educators. UMAP is funded by a grant from the National Science Foundation to Education Development Center, Inc., a publicly supported, nonprofit corporation engaged in educational research in the U.S. and abroad.

PROJECT STAFF

Ross L. Finney	Director
Solomon Garfunkel	Consortium Director
Felicia DeMay	Associate Director ,
Barbara Kelczewski	Coordinator for Materials Production
Paula M. Santillo	Assistant to the Directors'
Donna DiDuca	Project Secretary/Production Asst.
Janet Webber	Word Processor .
Zahcary Zevitas	Staff Assistant

NATIONAL STEERING COMMITTEE

W.T. Martin (Chair)		M.I.T.
Steven J. Brams		New York University
Llayron Clarkson		Texas Southern University
Ernest J. Henley		University of Houston •
William Hogan		Harvard University
Donald A. Larson		SUNY at Buffalo
William F. Lucas	,	Cornell University
R. Duncan Luce	•	Harvard University
George Miller	-	Nassau Community College
Walter E. Sears. 3		University of Michigan Press
George Springer		Indiana University
Arnold A. Strassenburg		SUNY at Stony Brook
Alfred B. Willcox		Mathematical Association of America

The Project would like to thank Douglas F. Hale of the University of Texas-Permian Basin, Odessa, Texas; Carol Stokes of Danville Area Community College, Danville, Illinois; Ray Treadway of Bennett College, Greensboro, North Carolina; Carroll O. Wilde of the Navai Postgraduate School, Monterey, California; and one anonymous reviewer, for their reviews, and all others who assisted in the production of this unit.

This material was prepared with the partial support of National Science Foundation Grant No. SED76-19615 A02. Recommendations expressed are those of the author and do not necessarily reflect the views of the NSF or the copyright holder.

1. INTRODUCTION

One of the major advantages in using a computer for problem solving is that a process can be explained to the computer once and the computer can repeat that process as many times as is necessary to solve the problem. In fact, without this computers would be of limited use as problem solving machines because it generally takes longer to explain a process to the computer than to carry it out by hand. Repeated execution of a single set of instructions on a computer is often called iteration. The term "iteration" also refers to any single execution of a process that is carried out more than once; the sense in which the term is used should be clear from the context.

The module describes ways in which you can use computer iteration effectively in problem solving and, in addition, ways in which you can use two other forms of iteration in constructing the algorithm. The second form of iteration involves repeated tracing through of the problem solving steps, improving your algorithm with each iteration. We call this process iterative improvement in algorithm design. Each improvement of the algorithm might add features to the previous version.

The third form of iteration in problem solving is found in an approach to algorithm design called the top-down approach. This approach for carring out step 4 of the problem solving process (see Unit 477) might best be called iterative refinement. It differs from iterative improvement in that the algorithm is not changed at each iteration, but rather, more detail is provided.

2. A MORTGAGE PROBLEM

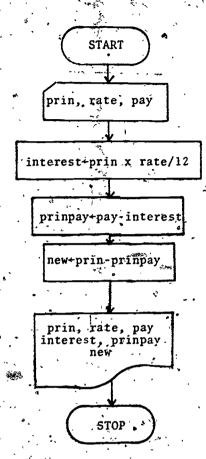
In order to illustrate the iteration technique, we shall solve the following problem: given an amount of

borrowed principal, a yearly interest rate, and a monthly payment, determine the new principal after one monthly payment has been made and determine the interest for one month.

The input for this algorithm consists of the principal at the beginning of the month, the yearly interest rate expressed as a decimal, and the amount of the payment. The output will consist of all values input plus the part of the payment which will be used to pay interest, the part of the payment which will be used to pay off the principal, and the new principal balance at the end of the month.

Algorithm 1. Mortgage payment - Version 1.

		Varia	bles •)
	Name ;	•	Description	
•	prin .	,	The principal balance at the	e
	•		beginning of the month.	
	rate-'	•	The yearly rate of interest	•
•		•	expressed as a decimal.	4
	pay	•	The amount of the payment.	
	interest	٠.	The part of the payment which	:ĥ
		•	goes toward interest.	
	prinpay		The part of the payment which	h
•			goes toward the principal.	. •
	new		The new principal balance at	the
	•	ē	end of the month.	



The interest is calculated by multiplying the principle, prin; times the interest rate divided by 12 because the given rate is for a year and the period used is a month. The value of prinpay is the amount left from the payment pay after the interest is paid. Finally, new is the principal balance after prinpay is paid.

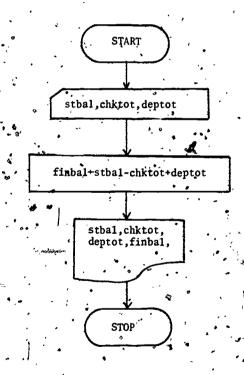
Exercises

1. Choose sample values for prin, rate, and pay, and follow through algorithm 4 as a computer would.

2. Follow the steps in the flowchart language algorithm below for some sample input values. The algorithm is one to balance a checkbook.

Algorithm: Balancing a checkbook

Name Description stbal Balance at the beginning of the month. Total amount of all checks written deptot Total amount of all deposits made during the month. finbal Balance at the end of the month.



. 3. ITERATIVE IMPROVEMENT

Although our mortgage payment algorithm 1 will function properly if friendly values are input, it will not respond in a suitable way to bad input. For example, consider the case in which the payment is too small to cover the interest for the month. Suppose prin = 20000., rate = .09, and pay = 100. If you follow through the steps of the algorithm with these values as input you get

interest = 150. prinpay = -50. new = 20050

On the other hand, the payment may also be too large. In this case, the payment covers the interest and the remaining principal and there is still some extra left. This is typical of the final payment in a pay-back schedule. For example, suppose prin = 60., rate = .09, and pay = 100. Then, the calculations would be

interest = 0.45. primpay = 99.55. new = -39.55.

We shall use iterative improvement to correct these two minor flaws in our original algorithm. If the payment is too small, we inform the user and terminate the program; if it is too large, we pay off the loan and notify the user that he or she is entitled to a refund.

These modifications to Algorithm 1 are indicated in Algorithm 2. The decision box included immediately after the input box tests for a payment too small to cover the interest. When this is the case, we provide a message to the user and then immediately halt the algorithm. This action represents a policy of disallowing payments which are inadequate to pay the interest.

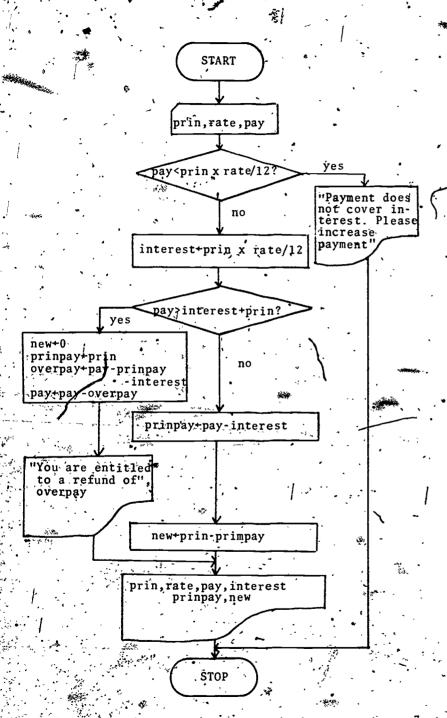
After the interest payment is calculated, we add another decision box which tests for payment greater than the principal. In this case, we calculate the new principal and amount paid on principal in a different way and adjust prinpay to exactly pay the remaining principal. We also include a message which notifies the user that he or she will receive a refund.

Algorithm 2. Mortgage payment - Version 2.

<u>Variables</u>

Name Description
The probability begins
rate The years
pay The arinterest The property goes to goes to

Description
The principal balance at the beginning of the month.
The yearly rate of interest expressed as a decimal.
The amount of the payment.
The part of the payment which goes toward interest.
The part of the payment which goes toward the principal.
The new principal balance at the end of the month.
The amount of overpayment for the final payment.



50

Exercises:

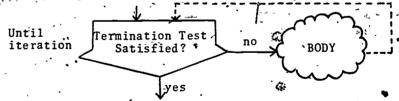
3. Follow through Algorithm 2 for the following input data:

••	Prin	rate	pay
Test 1	20000.	.12	250.
Test 2	20000.	.12	150.
Test 3	200.	.12	400.

4. ITERATION

The next step in the improvement of our mortgage algorithm will be to generate a schedule of payments by repeatedly executing the algorithm given above. To assist us in doing this, we use the three forms of iteration that were introduced in Section 1.

We shall discuss two forms of iteration here, and a third form in the next section. The first form will be called the *until iteration*. The iteration box which we use to describe this construction is indicated in the following diagram.

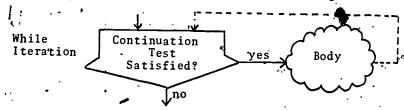


The body of the iteration is actually a subalgorithm which is to be repeated until the termination test is satisfied. The body of the iteration is shown as a cloud to indicate that this might be one or two boxes or a more involved set of flowchart statements. In the latter case, we will find it helpful to give the body a flowchart of its own and include only its name to the right of the iteration box. The procedure for doing that will be

discussed later. The dashed line from the body back to the termination test indicates that this is an automatic branch in the algorithm and not one that needs to be explicitly defined. We can consider the dashed line to be a part of the iteration box.

The second form of the iteration box is the while.

iteration. This form accomplishes exactly the same action as the until iteration but does it in a logically opposite way. Its general form is shown in the next diagram.



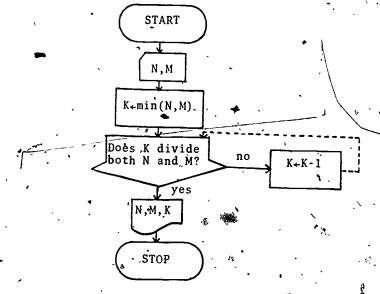
The test is now called a continuation test because the iteration is continued as long as the test is satisfied. The continuation test is always log ally opposite to the termination test; the two forms are introduced because some computer languages naturally perform the until iterations while others are designed for while iterations.

As an example of the use of the iterations, consider the algorithm for finding the greatest common divisor. We have two ways of expressing this algorithm using the iteration boxes just introduced.

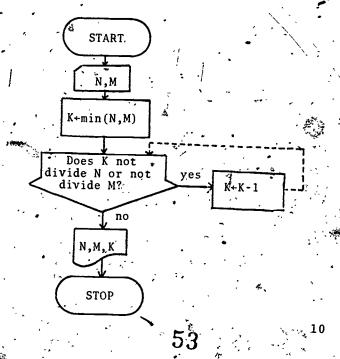
Algorithm 9. Given two numbers, N and M, find their greatest common divisor using an iteration statement.

variab,	<u>les</u>	
	Description	•
	The two numbers input to the	,
	, algorithm, ··	
	A counter which is tested for the	nę
	greatest common divisor.	,

a. Using until iteration



b. Using while iteration



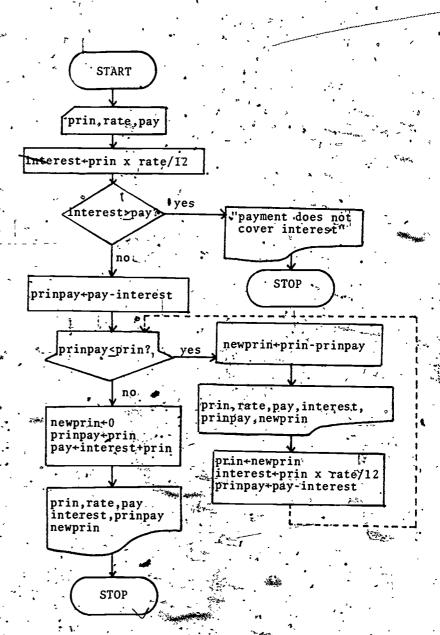
Algorithms 3a and 3b are logically equivalent in that they accomplish the same task. Note that the condition in the iteration box of Algorithm 3b is the logical negation of the one in the iteration box of Algorithm 3a. That is, you terminate precisely when you do not continue.

We now use these iteration boxes to make a final iterative improvement to our mortgage algorithm. We shall now have the algorithm continue to make monthly, payments until the mortgage is paid off. This algorithm is given in our flowchart language in Algorithm 4.

Algorithm 4. Generate the monthly payments necessary to pay off a mortgage with initial principal prin, yearly interest rate rate, and monthly payment pay.

Variables

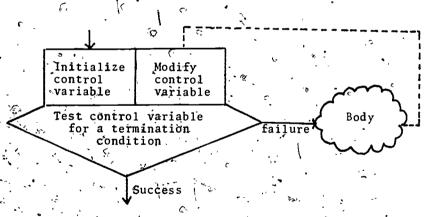
·*/	***************************************
<u>Name</u>	<u>Description</u>
prin	Principal amount.
rate	Yearly rate of interest ex-
	pressed as a decimal.
pay	Amount of the monthly payment.
interest	Part of the monthly payment
	which goes toward interest.
primpay	Part of the monthly payment
	which goes toward principal.
néwprin	New principal after a payment
	has been made.



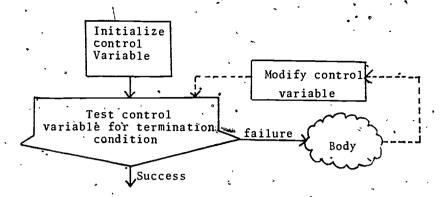
Much of this algorithm looks familiar from Algorithm 2. After the results for one month are printed in an iteration, that month's new principal is then set to be the next month's beginning principal. The iteration finally terminates when the amount paid on the principal exceeds the principal balance. Unlike Algorithm 2, we now call this a valid payment and make it the right amount to pay off the debt exactly.

5. VARIABLE-CONFROLLED ITERATION

In the last section we learned about forms of iteration which repeated a subalgorithm until termination conditions were met or continuation conditions were not. Now we introduce a slightly different form of iteration. This is iteration controlled by a variable. The general form of such an iteration is



It should be noted that this form of iteration is a special case of the form we studied in the preceding section. This iteration can be stated in terms of the previous one as indicated in the following diagram.

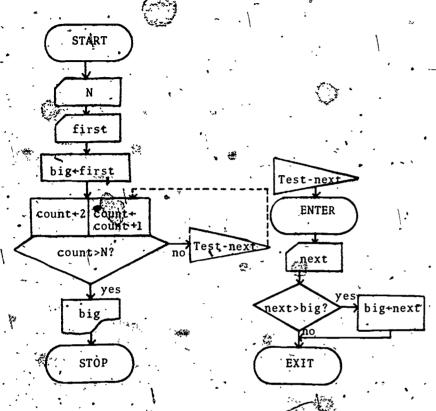


The reason we give the variable-controlled iteration its own form is that it is commonly used and is directly implemented in most programming languages.

The variable which controls the iteration is set to some initial value at the beginning of the iteration. It is then modified after each execution of the body and the iteration is terminated when the control variable satisfies some termination condition. In order to control the iteration properly, the control variable should not be changed in the body. This form of iteration is particularly useful when a process must be repeated a fixed number of times. In this case the control variable is used as a counter which in some way keeps track of the number of times the body has been executed.

Algorithm 5 provides an example of variable-controlled iteration. In this case, the variable count is used to count the number of data values which have been read in. It is initialized to 2 to indicate that the second value is read during the execution of the body. It is incremented by 1 each time, and when the increment makes count larger than N, then N values have been read, so the iteration is terminated.

Algorithm 5. Find the largest of N values.



Another new box has been introduced in this algorithm. This is the triangular shaped procedure box. The name inside such a box is the name of a procedure which is to be executed at that point. This type of box is used to avoid complicated constructions in the body of an iteration.

The flowchart for the procedure is then found elsewhere. Approcedure is actually a subalgorithm. Instead of beginning and ending with START and STOP boxes, its termination boxes are ENTER and EXIT. The ENTER box of a procedure has a pennant attached to it which gives the name by which it is called into action. When we arrive at the EXIT box of the procedure, we automatically cease execution of the procedure

and begin execution in the algorithm which called the procedure at the next sequential box after the procedure box.

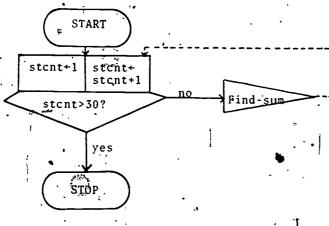
We will use such a procedure box as the body of a loop when the body is longer than one or two boxes.

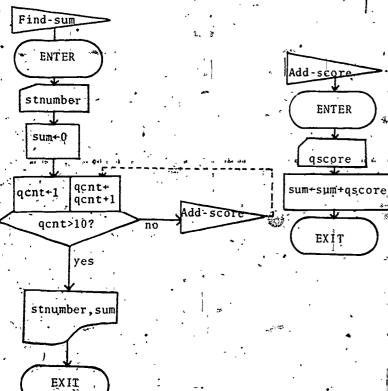
We now consider another example. Suppose there are 30 students in a class and each student has a student number and 10 quiz scores. The algorithm is to determine the sum of the quiz scores for each student. The algorithm for solving this problem is presented as Algorithm 6.

Here we have an iteration within an iteration. This is a construction that occurs frequently in algorithms. Also note, in the Find-sum procedure, that sum needs to be initialized to zero before a sum is accumulated. If this is not done, a cumulative sum of all students' scores will be computed. In fact, there is no guarantee that sum is zero at the very beginning of execution.

Algorithm 6 Find the sum of 10 quiz scores for each of 30 students.

Varia Varia	bles
Name	Description
stent	The counter for students which goes
	from 1 to 30.
stnumber	The student number read for each
in the second	student.
sum	The sum of each student's quiz
	SCOres.
qcnt	The counter for quizzes which goes
	from-1 to 10.
qscore	The quiz score read for each quiz
*	and student.



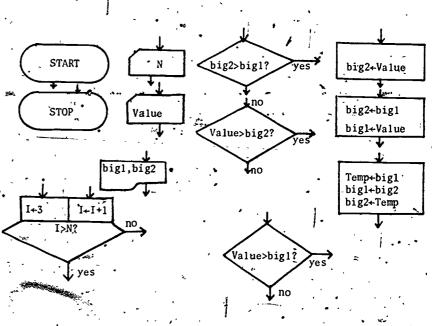


Exercises.

- 4. Modify algorithm 6 to input the number of students and the number of quiz scores for each student.
- 5. The following boxes are used in a flowchart language algorithm for finding the two largest numbers in a set of N numbers.

 Place the boxes in the proper arrangement.

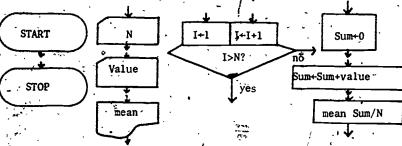
1.	Var	iables	<u>s</u> ,
Name	-,		Description
° N	لسال.	,	The number of values in the set.
Value	•	٠	The value read.
bigl			The biggest value read so far.
big2		•	The next-to-biggest value read so far.
I			A counter used to count the number of
	- , " " - f		values read.



6. The following boxes can be used to construct an algorithm for computing the mean of a set of N numbers. Arrange them in the proper order.

. Variables

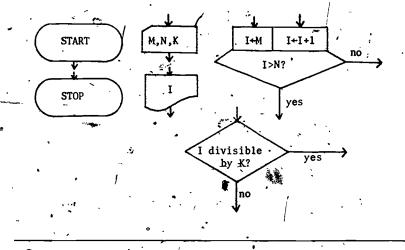
,	Name	Description
	N	The number of values in the set.
-	Value `	The value read.
	Mean	The mean of the values.
	I	A counter used to count the number of values
.*	, *	read.
	Sum	The sum of the values read.



7. Arrange the following boxes to form an algorithm which finds all integers between M and N which are exactly divisible by K.

<u>Variables</u>

•	VALIABICS	· · · · · · · · · · · · · · · · · · ·
ame	7	Déscription
		The lower limit of the range of integers.
		The upper limit of the range of integers.
٠		The value whole numbers are to be printed.
	, ř.	A counter used to test for answers which
	1	goes from M to N.



TOP-DOWN APPROACH

The top-down approach for designing algorithms is a technique that allows the designer to handle a complicated algorithm in a simple way. The esic approach is to design the algorithm using powerful boxes, then breaking those boxes down into flowcharts with less powerful boxes and continuing that process until you are at a level suitable for implementation on a computer.

In order to illustrate this technique, we look at an algorithm for arranging N numbers in natural order.

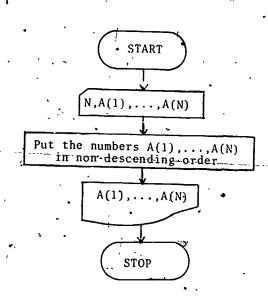
Algorithm 7. Read N numbers and print them in non-descending order.

Variables.

Name Description

The number of values in the set.

An array of N values to be ordered.

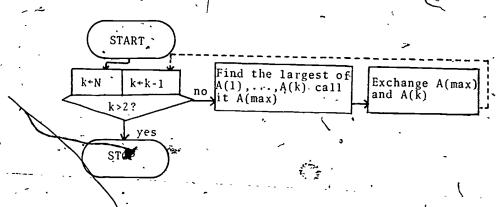


This is obviously not the final solution to our problem since we still have not described the process in engugh detail for the computer to follow. The next step is to break the middle box itself down into an algorithm.

This is the beginning of iterative refinement.

Algorithm 8. Put the numbers $A(1), \dots, A(N)$ into non-descending order.

·	Variables	
Name	1 1	Description
N A		The number of values in the set. An array of N values to be
-k		ordered. A counter which goes from Nato 2.
max		The index of the largest value from A(1) to A(k).



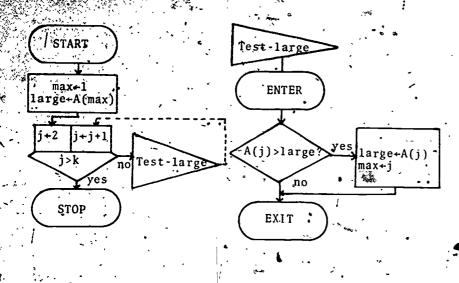
This procedure, for k=N down to k=2, is to find the largest of the first k values and place it at the kth position. The first time, with k=N, we find the largest in the entire set and put it at the bottom. The next pass through the iteration, with k=N-1, we ignore A(N) since it is already correct, and place the largest of the first N-1 values in the (N-1)st position. We continue the process until all are in order.

Next we break down the box "find the largest..." into a flowchart.

Algorithm 9 it A(max). Find the largest of A(1), ..., A(k), call

•-	Variables
Name -	Description
Α'	An array of values.
k ·	The number of values in the set.
max.	The index of the largest value from
0	'A(1) to A(k)
large `	The value of A(max).
' j '	A counter which goes from 2 to k.

2]



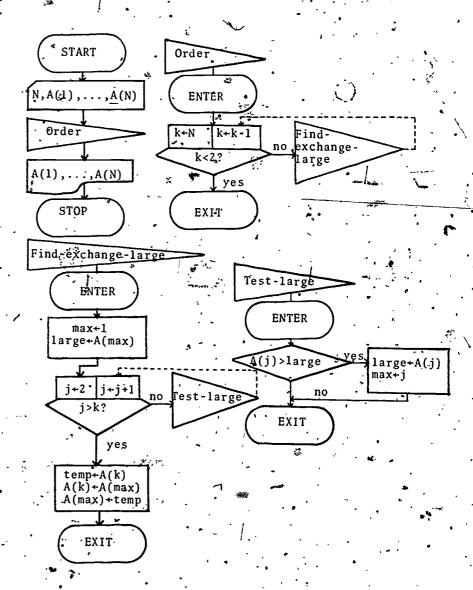
Finally, we expand the "Exchange..." box from Algorithm 9. This requires three data movements and one temporary location. It is given by the following algorithm.

Algorithm 10. Exchange A(max) and A(k).

Variables ·

1 <u>v</u>	ariables	•	′ 、 •		•
Name -	<u>Desc</u>	ription		٠.	٠.
A K, max	-	array of val	•	Values t	ď
1		exchanged		•	
	STAR	et .		*** .	
	temp+A A(k)+A A(max)	(max)			•
	STO				

We now have, in Algorithms 7-10, all of the steps necessary to complete the task of placing the numbers in Orders. We combine these into one flowchart for Algorithm Algorithm 11. Complete Algorithm to read N numbers and print them in non-descending order.



Algorithm 11 was designed by the top-down approach. This means that we start with the highest level tasks and proceed to break them down into more and more detailed subtasks until finally we have an algorithm which is detailed enough to provide complete instructions to computers. In this way we have broken the original problem down into three simpler problems.

In general, top-down design is an approach whereby a difficult problem is broken down into several simpler problems. Each of these simpler problems may also be broken down into several simpler ones, and so on until all of the problems to be solved are within the grasp of the problem solver. This iterative refinement is a very important strategy in computer problem solving.

Exercises:

8. Using the set of numbers 5,3,9,6,2,7 follow through Algorithm 11 as a computer would.

7. SOLUTIONS TO EXERCISES

3. For Test 1, result is prin = 20000.

rate = .12

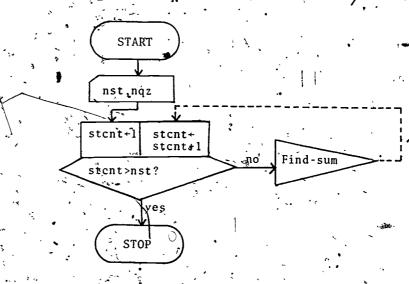
pay = .250...

interest = 200

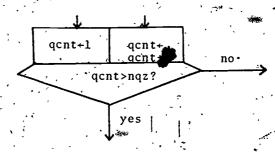
prinpay = 50...

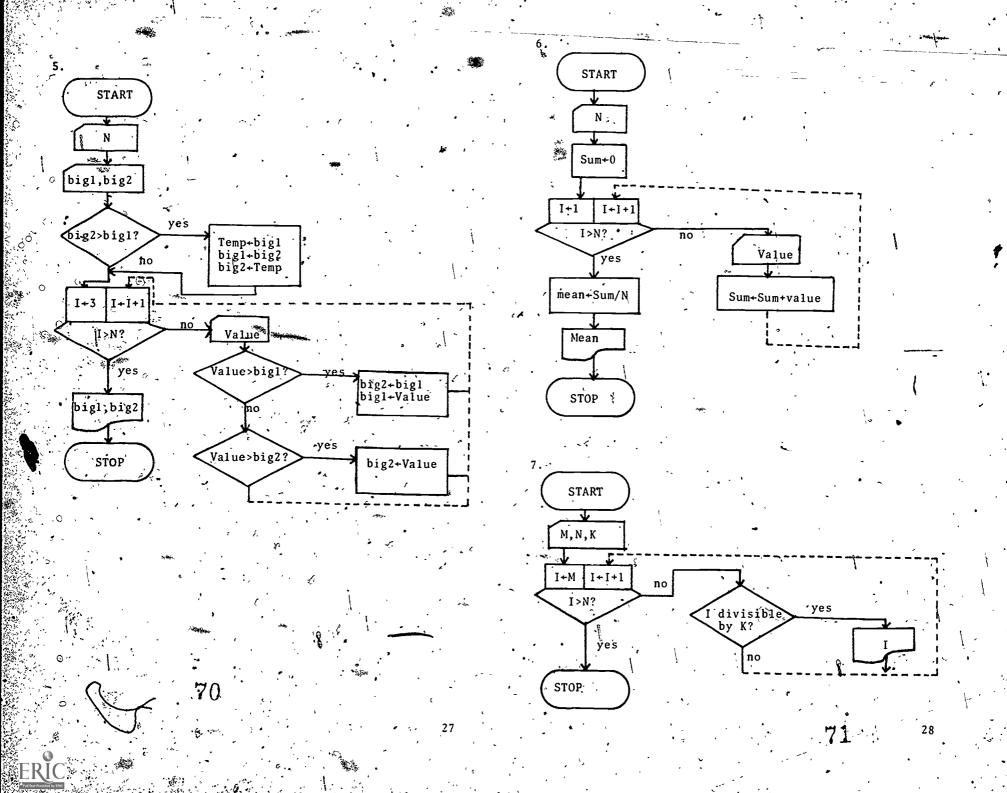
new = 19950.

4. Change first flowchart to;



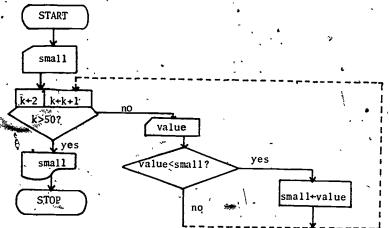
Change iteration box in Find-sum to



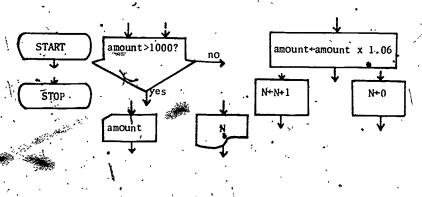


8. MODEL EXAM

1. The following algorithm reads a set of 50 numbers and prints the smallest number in the set. Modify the algorithm so that it prints not only the smallest number, but also the number of times that number occurs in the set.

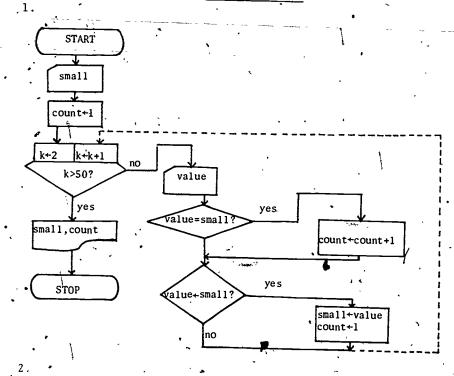


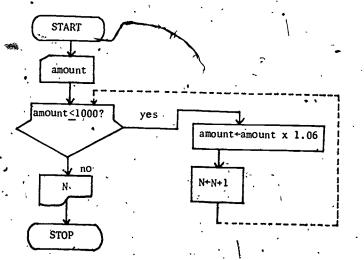
Write an algorithm which reads an amount of money and determines how many years it would take for that amount to grow to over \$1000 if it accumulates interest at the rate of 6% compounded annually. Use each of the boxes below exactly once.



Explain in your dwn words the top-down approach to algorithm design. Discuss why it is important.

9. SOLUTIONS TO MODEL EXAM





29

30.

72

Request for Help

EDC/UMAP 55 Chapel St. Newton, MA 02160

Your Name Page	out this form and tak	trouble with a specific part of the it to your instructor, for assist	: This unit, please fill Tance. The information
Page O Upper OMiddle O Lower Description of Difficulty: (Please be specific) Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	. you give will neip th	e author to revise the unit.	
O Upper OMiddle O Lower Description of Difficulty: (Please be specific) Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: O ave student better explanation, example, on procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not. using examples from this unit.)			. Unit No.
O upper OMiddle O Lower Description of Difficulty: (Please be specific) Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem—solving skills (not, using examples from this unit.)	Page		Model Exam
Description of Difficulty: (Please be specific) Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	O Upper OP		1
Description of Difficulty: (Please be specific) Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	The state of the s		-
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	2.		1
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	Description of Diffic	ulty: (Please he specific)	
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)		arty. (Trease be specific)	
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	· •-	•	•
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)		•	
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	•		
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	,		
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	,		. ø
Instructor: Please indicate your resolution of the difficulty in this box. Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.)	•		3
Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature	· · · · · · · · · · · · · · · · · · ·		
Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature		, , ,	, , , , , , , , , , , , , , , , , , ,
Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature			·
Corrected errors in materials. List corrections here: Gave student better explanation, example, or procedure than in unit. Give brief outline of your addition here: Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature	***		
Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature	Corrected erro	rs in materials. List corrections	here:
Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature			1
Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature		•	.) .
Assisted student in acquiring general learning and problem-solving skills (not using examples from this unit.) Instructor's Signature	<i>y</i> .		•
skills (not.using examples from this unit.) Instructor's Signature			•
skills (not.using examples from this unit.) Instructor's Signature	^	•	•
skills (not.using examples from this unit.) Instructor's Signature		•	· · · · ·
skills (not.using examples from this unit.) Instructor's Signature			
skills (not.using examples from this unit.) Instructor's Signature	•	•	,
skills (not.using examples from this unit.) Instructor's Signature		• • •	•
Instructor's Signature			and problem-solving
instructor s Signature			,
instructor s Signature		· ·	•
instructor s Signature	•		
instructor s Signature		74	
instructor s Signature			
		Instructor's Signature	

Please use reverse if necessary.

STUDENT FORM 2 Unit Questionnaire

Return to: EDC/UMAP 55 Chapel St. Newton, MA 02160

Name	Unit No	Date	
Institution	Course No		×
Check the choice for each question	that comes closest	to your personal opin	ion.
1. How useful was the amount of de	tail in the unit?	,44	,
Not enough detail to unders Unit would have been cleare Appropriate amount of detai Unit was occasionally too d Too much detail; I was ofte	r with more detail l etailed, but this w	as not distracting	1
2. How helpful were the problem an	euoro?		
•			•
Sample solutions were too b Sufficient information was Sample solutions were too d	given to solve the	problems	eps
3. Except for fulfilling the prere example, instructor, friends, or	quisites, how much r other books) in o	did you use other sourder to understand th	rces (for e unit?
A LotSomewhat	A Littl	eNot at	ali
4. How long was this unit in compa a lesson (lecture and homework			
Much Somewhat Longer Longer	About the Same	Somewhat Much Shorter Shor	-
5. Were any of the following parts as many as apply.)	of the unit confus	ing or distracting? (Check
Prerequisites Statement of skills and con Paragraph heading Examples Special Assistance Suppleme Other, please explain		· · · · · · · · · · · · · · · · · · ·	
6. Were any of the following parts as apply.) Prerequisites Statement of skills and con Examples Problems	• .	ularly helpful? (Chec	ck as many
Paragraph headings Table of Contents Special Assistance Suppleme Other, please explain	nt (if present)	* * *	. <i>I</i> • (

Please describe anything in the unit that you did not particularly like.

Please describe anything that you found particularly helpful. (Please use the back of this sheet if you need more space.)